

# Distributed Verification of Modular Systems

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# Motivation

Exhaustive analysis of complex systems using state spaces  
⇒ state space explosion problem

## Coping with state space explosion

- Reduction of the state space
  - symmetries
  - partial orders
  - sleep sets, etc.
- Reduction of the representation
  - BDDs, DDDs, etc.
  - modular state spaces
  - distributed state spaces

## Aims

Combine modular and distributed approaches

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# Outline

- 1 Characteristics of Modular Distributed state space generation
- 2 Properties verification
- 3 Experiments
- 4 Conclusion and future work

# State space generation

## Modular state spaces

### Local state spaces

- specific to a module
- only local behaviour

### Synchronisation graph

- global behaviour (fused transitions)
- nodes represent sets of states linked by local actions

## Distributed architecture

- Coordinator
- initiates the computation
  - handles termination

- Workers
- compute part of the state space
  - collaborate via message passing



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### Workers

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# Modular distributed state space generation

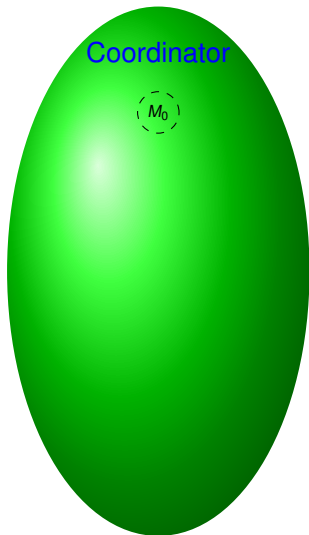
## Coordinator

- builds the **synchronisation graph**
- **coordinates** the worker processes
- ensures **termination**

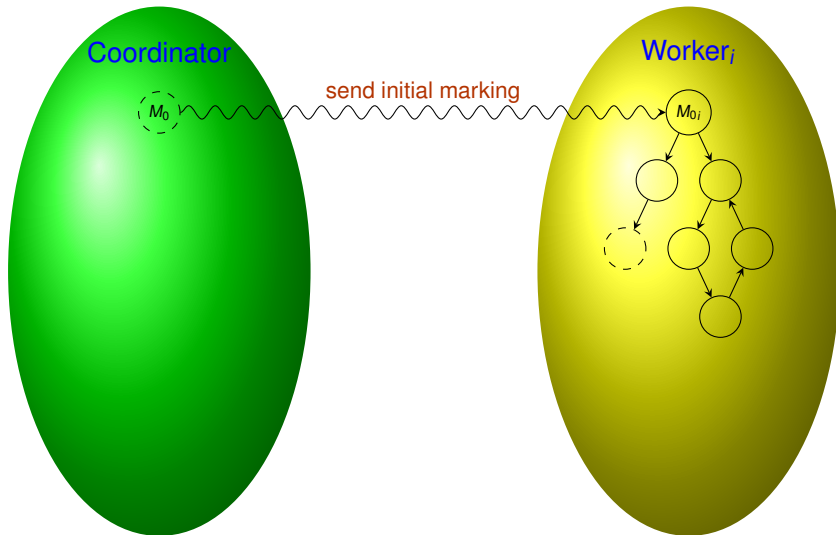
## Workers

- constructs the **local state space**
- sends possible **synchronisation points** to the coordinator

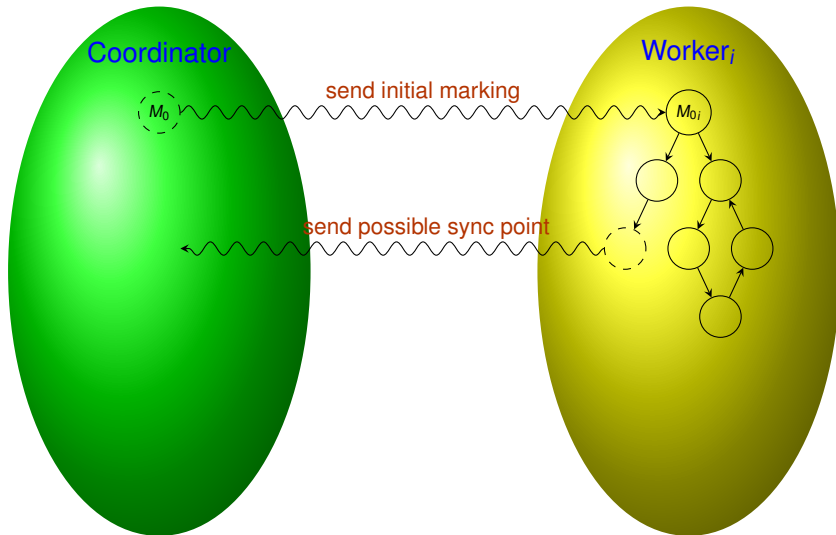
# Distributed state space generation



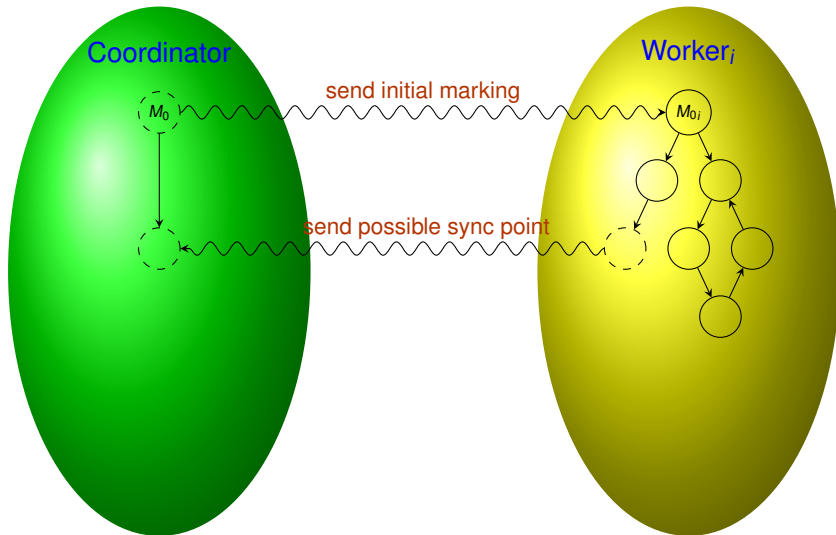
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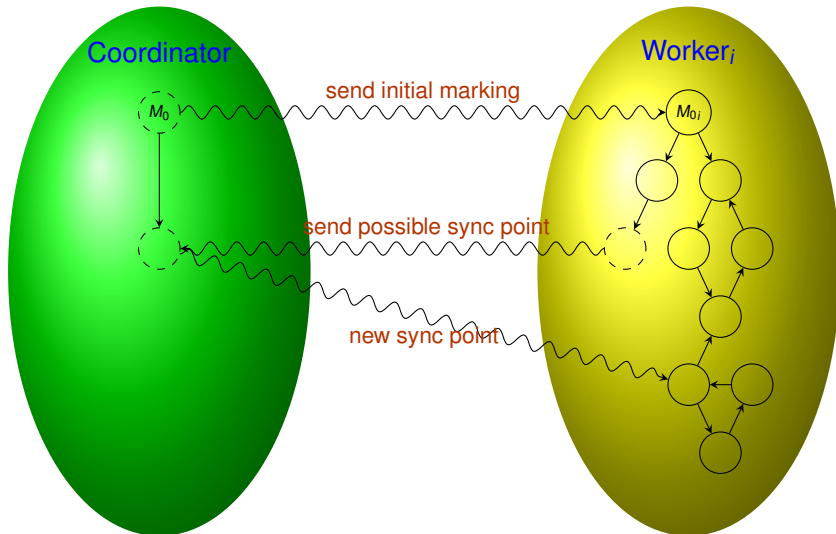
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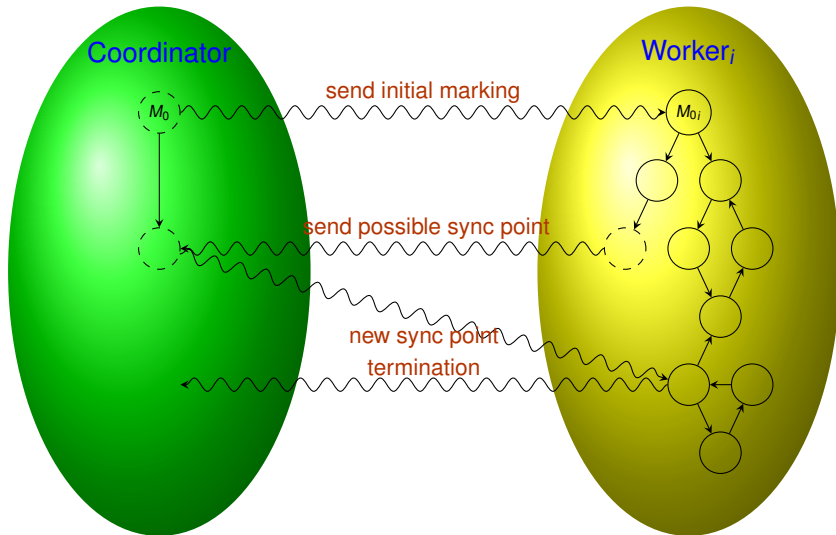
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# Main characteristics

**SCCs** of local state spaces are updated during the construction

**Messages** contains the fused transition enabling and the **SCCs** of its markings

**Synchronisation** only focuses on participating modules

**Termination** occurs when all workers have finished computing their local state space, and there is no new synchronisation point

# Verifying properties

- as much local computation as possible
- minimise the number of messages exchanged by worker processes

# Reachability

## Global part (Coordinator)

- **sends partial markings** to the worker processes
- If it receives a negative answer the marking is not reachable
- otherwise find a combination of the ancestor SCCs in the synchronisation graph

## Local part (Worker processes)

- search for their partial marking in their local state space
- If it is not found the marking is not reachable
- otherwise send its ancestor SCCs to the coordinator

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# Deadlocks

## Global part (Coordinator)

- find a combination of dead markings received on the arcs of the synchronisation graph
- If it does not label an arc but is reachable, then it is a deadlock

## Local part (Worker processes)

- search for dead markings in their local state space
- If there is none the system is deadlock-free
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# Liveness — Fused transition $tf$

## Global part (Coordinator)

- If there exists a **terminal SCC** in the synchronisation graph **not containing  $tf$**  then  $tf$  is not live
- **otherwise send nodes of the synchronisation graph to the worker processes**
- if a combination of nodes received does not label an arc in the synchronisation graph,  $tf$  is not live

## Local part (Worker processes)

- receive  $v_s$
- send terminal SCCs reachable from  $v_s$  to the coordinator



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- receive  $v_s$
- identify terminal SCCs that do not enable  $t$
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# Experimental results

## Setting for experiments

- 1 machine for the coordinator process
- 11 for the worker processes
- philosophers and AGVs examples

## Analysis of results

- significant gain in time during the construction
- few messages exchanged for the construction and reachability properties
- optimisation for liveness and home states, so as to decrease the number of messages

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# Conclusion & Future work

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- distributed modular state spaces
- distributed modular analysis

## Future work

- apply to larger case studies
- extension to temporal logic properties



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